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ABSTRACT

A method for comparing the cross-validated classification accuracies of predictive discriminant analysis and logistic regression classification models is presented under varying data conditions for the two-group classification problem. With this method, separate-group, as well as total-sample proportions of the correct classifications, can be compared for the two models. The test for contrasting correlated proportions developed by Q. McNemar (1947) is used in the statistical comparisons of the separate-group data and total-sample proportions. The method is illustrated with 32 real data sets that varied in number of cases, relative group sizes, number of predictor variables, degree of group separation, and equality of group covariance matrices. (Contains 1 table and 24 references.) (SLD)

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Predictive Discriminant Analysis Versus Logistic Regression in Two-Group Classification Problems

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Predictive Discriminant Analysis Versus Logistic Regression in Two-Group Classification Problems

ABSTRACT. A method for comparing the cross-validated classification accuracies of predictive discriminant analysis and logistic regression classification models is presented under varying data conditions for the two-group classification problem. With this method, separate-group as well as total-sample proportions of correct classifications can be compared for the two models. McNemar's test for contrasting correlated proportions is used in the statistical comparisons of the separate-group and total-sample proportions. The method is illustrated with 32 real data sets.

Among the methods used for solving two-group classification problems, logistic regression (LR) and predictive discriminant analysis (PDA) are two of the most popular (Yarnold, Hart, & Soltysik, 1994, p. 73). Unlike PDA, LR captures the probabilistic distribution embedded in dichotomous measures, avoids violations to the assumption of homogeneity of variance, and does not require strict multivariate normality (e.g., see Aldrich & Nelson, 1984; Cox & Snell, 1989). Therefore, when PDA assumptions are violated, we might theoretically expect higher cross-validated classification hit rate accuracy with LR than PDA.

Although several studies have compared the classification accuracy of LR and PDA, the results have been inconsistent. For example, results of three simulation studies (Barón, 1991; Bayne, Beauchamp, Kane, & McCabe, 1983; Crawley, 1979) suggest that LR is more accurate than PDA for nonnormal data. However, several researchers (e.g., Cleary & Angel, 1984; Dey & Astin, 1993; Knoke, 1982; Krzanowski, 1975; Press & Wilson, 1978) using nonnormal real data found little or no difference in the accuracy of the two techniques. Findings are also inconsistent for degree of group separation. Bayne, et al. (1993) found that larger group separation favored PDA, while Crawley (1979) found this condition to favor LR. Sample size is yet another data condition yielding inconsistent results. In a simulation study, Harrell and Lee (1985) found that PDA was more accurate than LR for small samples. By contrast, in a study by Johnston and Seshia (1992) using real data, LR worked better than PDA for small samples.

Given these inconsistencies in the literature, it is not clear which of the two methods will work better for a given data set. Consequently, a method for comparing the accuracy of PDA and LR for a specific data set will enable researchers to select the optimal classification procedure for that data set. In this paper we describe a method for determining the superior classification model for a specific data set,

regardless of data conditions. In addition, a computer program that accomplishes the method is introduced and demonstrated.

Method

Data Sources. We used 32 classification data sets varying in number of cases, relative group sizes, number of predictor variables, degree of group separation, and equality of group covariance matrices to illustrate the method. To bolster validity, all were taken from real classification studies. The sources include journal articles, paper presentations and research texts.

Procedure. For PDA, we built linear classification functions based on assumptions of multivariate normality, equal covariance matrices, and equal prior probabilities of group membership. We classified cases into groups using Tatsuoka's (1988) minimum chi square rule. For LR, we used the elegant IMSL subroutine CTGLM, conveniently available with the powerful new 32-bit Microsoft Fortran v4.0 Powerstation, to obtain model coefficients. The CTGLM routine uses a standard nonlinear approximation technique (Newton-Raphson) to determine maximum likelihood estimates of model coefficients. We classified each case into the group with the highest log-likelihood probability.

In comparing the predictive accuracy of the PDA model to that of the LR model, we considered external rather than internal results. Results of an internal classification analysis are those obtained when measures for the individuals on whom the statistics were based are resubstituted to obtain the predicted classification scores. In an external classification analysis statistics based on one set of individuals are used in classifying new individuals. An external analysis is appropriate for making inferences about the discriminatory power of the predictors for a new set of data (Huberty, 1994).

We estimated external, or cross-validated, hit-rate accuracy using the leave-one-out procedure. A case is classified by applying the model derived from all cases except the one being classified. This process was repeated round-robin for each case with a count of the overall classification accuracy used to estimate the cross-validated accuracy. This procedure has a relatively wide following in the discriminant analysis literature (see, for example, Huberty, 1994; Huberty & Mourad, 1980; Lachenbruch, 1967; Mosteller & Tukey, 1968).

We compared separate-group as well as total-sample proportions of correct classification for the PDA and LR models. We used McNemar's (1947) test for contrasting correlated proportions in the statistical comparisons between PDA and LR

models for the separate-group and total-sample proportions. This method was previously suggested for comparing full and reduced classification methods (Morris & Huberty, 1995; Morris & Meshbane, 1995) as well as for comparing linear and quadratic classification models (Meshbane & Morris, 1995), but is equally applicable in comparing PDA and LR models. (See Looney, 1988, for a method of comparing classification results of more than two models.) Because the calculation of the McNemar correlated proportion statistic requires the joint distribution of hits and misses for both the PDA and LR models, no statistical package will accomplish the method. Therefore, we wrote a FORTRAN computer program to provide this information.

We used the Box test for testing the assumption of homogeneity of covariance structures. This test is sensitive to multivariate normality, and the outcome is therefore confounded with the homogeneity of dispersion issue. Nevertheless, the Box test is routinely used for testing the homogeneity of dispersion assumption and is even the default in some statistical packages. Notwithstanding concerns over this test, once could argue that, theoretically, a logistic classification model is more likely to be appropriate when the Box test indicates that the covariance structures are unequal.

Results and Discussion

For each of the data sets, Table 1 gives a short description, the degree of group separation (D), the number of cases in group 1 (n_1), the number of cases in group 2 (n_2), an index of disproportionality of the group sizes (I) calculated as (n_i * 100) / n_j, where n_i is the larger of the two groups, the number of predictor variables (p), results of the Box test for homogeneity of covariance structures, and a comparison of the leave-one-out performance of the PDA and LR models for each group separately and for the total sample. We compared the performance of the two classification models, displayed as the hit-rate percentage obtained by the p predictor variables, via McNemar's test for contrasting correlated proportions.

To make an inferential decision using this method, the researcher must, as is customary, choose an alpha level; the choice of alpha level results in an associated critical z statistic. To illustrate the method for these data sets, we used the .01 alpha level with the associated z of 2.58.

In the first three data sets, maximum likelihood estimates of logistic regression parameters could not be calculated due to complete separation of the data (see Table 1). Among the remaining 29 data sets, differences between the PDA and LR models in classifying the total sample were not statistically significant, with the exception of

Data Set 26 (see Table 1). Here, the LR model yielded a significantly higher total hit rate.

Insert Table 1 about here

Differences between the two classification models in separate-group hit rates were statistically significant in nine of the 32 data sets (9, 16, 17, 23, 24, 26, 30, 31, and 32). In eight of these data sets, superior performance of the LR model in classifying the larger group was offset by superior performance of the PDA model in classifying the smaller group; the only exception was Data Set 31, in which the significant advantage of the LR model for the larger group was offset by a nonsignificant advantage of the PDA model for the smaller group.

Statistically significant differences in separate-group hit rates were found in data sets with moderate to relatively large discrepancies in sample sizes and small to moderate group separation, but not in any data set with similar sample sizes ($I < 118$) nor in any data set with relatively large group separation ($D > 2.0$). This indicates that CTGLM uses sample sizes as estimates of population sizes when generating maximum likelihood estimates of LR model parameters. Using sample sizes as estimates of population sizes is inappropriate, however, when population sizes are unknown or when sample sizes are not proportional to population sizes (Huberty, 1994, p. 65). Consequently, we decided to force the assumption of equal population sizes by adjusting the LR model by a constant. We determined the value of the constant by referring to the FORTRAN program LOGDIS (Albert & Harris, 1987), which uses an iterative Newton-Raphson procedure to obtain maximum likelihood estimates of LR model parameters for the k-group classification problem. Under the assumption of equal population sizes, there were no statistically significant differences in total-sample or separate-group hit rates between LR and PDA for any of the 29 data sets for which maximum likelihood estimates of LR model parameters could be calculated (results available on request).

Therefore, from the perspective of these data sets, which were selected to portray a wider range of characteristics than were previously available, some evidence can be tentatively gleaned. For total-group accuracy, hit rates for the LR and PDA models were the same in 28 of the 29 data sets for which LR model estimates could be calculated. Neither theoretical nor data-based considerations were helpful in predicting which of the two models would work better.

In reference to separate-group accuracy the results are a bit more complicated. For separate-group hit rate to be of interest the researcher must make an a priori decision that accuracy in one group is more important than in the other. For example, the researcher may decide that, in predicting high school dropouts, to be correct for the dropouts is more important than for a persister group. These data suggest that when the size of one population is much larger than the other, the researcher may improve separate-group hit rate by choosing the LR model if interest is in classification accuracy of the larger group, and by choosing the PDA model if interest is in classification accuracy of the smaller group.

It certainly may be that there are other data sets in which LR or PDA would be judged significantly superior for total-group as well as separate-group hit rates; from the results of these analyses, it seems quite possible that there may be data that manifest a PDA rule that is significantly superior for one group and an LR rule that is significantly superior for the other. In this case, if the researcher has interest in separate group accuracy, knowledge of these results would allow selection of a rule depending on which group is of highest superiority. Use of the method and computer program demonstrated herein will allow such decisions to be made based on explicit cross-validated classification accuracies.

Note

For a copy of the FORTRAN program that accomplishes the method, send a returnable diskette and diskette mailer to Alice Meshbane, College of Education, Florida Atlantic University, P.O. Box 3091, Boca Raton, FL 33431-0991. Internet: Meshbane@acc.fau.edu.

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Table 1

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
1	Fisher Data - Groups 1 & 3	13.97	100	50	50	4	$\chi^2 = 6.9057$, $p < .0001$ $df = 10$	PDA LR McNemar's z	100 *	100 *	100 *
2	Fisher Data - Groups 1 & 2	10.16	100	50	50	4	$\chi^2 = 5.0455$, $p < .0001$ $df = 10$	PDA LR McNemar's z	100 *	100 *	100 *
3	Bisbey Data - Groups 1 & 3	5.12	106	35	37	13	$\chi^2 = .9939$, $p = .5013$ $df = 91$	PDA LR McNemar's z	97 *	94 *	100 *
4	Fisher Data - Groups 2 & 3	3.77	100	50	50	4	$\chi^2 = .7148$, $p = .7125$ $df = 10$	PDA LR McNemar's z	93 91 .82	92 92 .00	94 90 1.41

* Due to complete separation of the data, maximum likelihood estimates of LR model parameters could not be calculated.

Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
5	Junior Faculty Performance Data	3.11	152	27	41	4	$\chi^2 = 2.2172$, $p = .0150$	PDA	91	93	90
							$df = 10$	LR	93	89	95
								McNemar's z	-.58	1.00	-1.41
6	Rulon Data - Groups 1 & 3	2.93	129	85	66	4	$\chi^2 = 3.4973$, $p = .0003$	PDA	93	94	91
							$df = 10$	LR	91	93	89
								McNemar's z	1.41	1.00	1.00
7	Bisbey Data - Groups 1 & 2	2.89	231	35	81	13	$\chi^2 = 1.0021$, $p = .4777$	PDA	89	89	89
							$df = 91$	LR	88	83	91
								McNemar's z	.58	1.41	-1.00
8	Bisbey Data - Groups 2 & 3	2.41	219	81	37	13	$\chi^2 = 1.2131$, $p = .0929$	PDA	84	83	87
							$df = 91$	LR	86	89	78
								McNemar's z	-.63	-1.89	1.73

Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
9	Talent Data - Groups 3 & 5	1.97	285	33	94	14	$\chi^2 = 1.1086$, $p = .2238$	PDA	77	79	77
							$df = 105$	LR	79	58	86
								McNemar's z	-.50	2.65	-3.00
10	Demographic # 2 - Body Char	1.88	129	157	122	8	$\chi^2 = 6.6870$, $p < .0001$	PDA	82	83	82
							$df = 36$	LR	81	83	77
								McNemar's z	1.89	-1.00	2.45
11	Rulon Data - Groups 2 & 3	1.87	141	93	66	4	$\chi^2 = 3.4962$, $p = .0003$	PDA	83	85	80
							$df = 10$	LR	82	87	76
								McNemar's z	.45	-1.41	1.73
12	Rulon Data - Groups 1 & 2	1.74	109	85	93	4	$\chi^2 = 4.9003$, $p < .0001$	PDA	81	84	79
							$df = 10$	LR	80	80	81
								McNemar's z	.45	1.73	-1.41

Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
13	Talent Data - Groups 1 & 5	1.72	113	83	94	14	$\chi^2 = 1.5086$, $\underline{p} = .0014$	PDA	75	74	76
							$\underline{df} = 105$	LR	74	74	75
								McNemar's $\underline{z}$	1.00	.00	-1.00
14	Demographic # 3 - Body Char	1.36	104	142	137	8	$\chi^2 = 5.2724$, $\underline{p} < .0001$	PDA	73	70	76
							$\underline{df} = 36$	LR	73	72	74
								McNemar's $\underline{z}$	.38	-1.41	1.34
15	Press & Wilson - 50 States	1.31	100	25	25	5	$\chi^2 = 2.6544$, $\underline{p} = .0008$	PDA	64	68	60
							$\underline{df} = 15$	LR	70	72	68
								McNemar's $\underline{z}$	-1.13	-.58	-1.00
16	Business Sch Perf Data - 1990	.89	188	147	78	7	$\chi^2 = 1.5719$, $\underline{p} = .0300$	PDA	64	61	69
							$\underline{df} = 28$	LR	67	83	37
								McNemar's $\underline{z}$	-1.05	-5.74	5.00

Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
17	Talent Data - Groups 1 & 3	.89	252	83	33	14	$\chi^2 = .9401$, $p = .6493$	PDA	58	64	42
							$df = 105$	LR	62	81	15
								McNemar's z	-1.04	-3.74	3.00
18	Block Data - Groups 3 & 4	.85	100	38	38	4	$\chi^2 = 4.3098$, $p < .0001$	PDA	68	74	63
							$df = 10$	LR	68	71	66
								McNemar's z	.00	.58	-1.00
19	Block Data - Groups 1 & 2	.84	105	40	38	4	$\chi^2 = 2.2028$, $p = .0157$	PDA	68	60	76
							$df = 10$	LR	69	65	74
								McNemar's z	-.58	-1.41	1.00
20	Block Data - Groups 1 & 4	.81	105	40	38	4	$\chi^2 = 1.5500$, $p = .1163$	PDA	60	58	63
							$df = 10$	LR	58	58	58
								McNemar's z	1.41	.00	1.41

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Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
21	Higher Ed Persistence Data	.76	102	263	269	11	χ^2 = .9860, p = .5101	PDA	62	62	61
							df = 10	LR	61	61	61
								McNemar's z	1.13	2.00	-.58
22	Block Data - Groups 1 & 3	.74	103	40	39	4	χ^2 = 5.3857, p < .0001	PDA	65	58	72
							df = 10	LR	62	58	67
								McNemar's z	1.41	.00	1.41
23	MBA Success Data - 1986	.72	144	64	92	7	χ^2 = 1.2640, p = .1632	PDA	64	66	62
							df = 28	LR	58	36	73
								McNemar's z	1.67	4.36	-3.16
24	Warncke Data - Groups 1 & 3	.69	163	65	40	10	χ^2 = 1.5335, p = .0086	PDA	57	62	50
							df = 55	LR	60	79	30
								McNemar's z	-.69	-3.32	2.83

Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
25	MBA Success Data - 1989	.69	114	66	75	7	χ^2 = .6058, p = .9480	PDA	60	61	59
							df = 10	LR	59	53	64
								McNemar's z	.33	2.23	-2.00
26	Business Sch Perf Data - 1989	.66	246	160	65	7	χ^2 = .9730, p = .5060	PDA	56	54	63
							df = 28	LR	69	94	08
								McNemar's z	-2.80	-8.00	6.00
27	Block Data - Groups 2 & 3	.64	105	37	39	4	χ^2 = 4.5542, p < .0001	PDA	55	57	54
							df = 10	LR	57	54	59
								McNemar's z	-.58	1.00	-1.41
28	Block Data - Groups 2 & 4	.52	103	37	38	4	χ^2 = 1.2033, p = .2838	PDA	59	62	55
							df = 10	LR	57	65	50
								McNemar's z	.00	.00	.00

Table 1, cont.

Data Set Description, Results of Box M Test for Equality of Covariance Matrices, and Comparison of Hit Rate Percents for PDA and LR Models

#	Data Set Description	D	I	n_1	n_2	p	Results of Box M Test for Equal Covariance Matrices	Model Used	L-O-O Hit Rate % Total	GR 1	GR 2
29	Demographic # 1 - Body Char	.50	104	137	142	8	$\chi^2 = 5.4808$, $p < .0001$	PDA	58	61	55
							$df = 36$	LR	58	58	58
								McNemar's z	.00	2.00	-2.00
30	Warncke Data - Groups 1 & 2	.48	138	65	47	10	$\chi^2 = 1.0593$, $p = .3611$	PDA	48	51	45
							$df = 10$	LR	45	68	13
								McNemar's z	.78	-3.32	3.87
31	Warncke Data - Groups 2 & 3	.45	118	47	40	10	$\chi^2 = 1.2556$, $p = .1039$	PDA	40	45	35
							$df = 55$	LR	43	60	23
								McNemar's z	-.58	-2.65	2.24
32	Enrollment Data	.39	157	272	426	4	$\chi^2 = 83.2884$, $p = .0000$	PDA	60	58	61
							$df = 10$	LR	62	28	84
								McNemar's z	-1.28	8.94	-9.85